

PROBLEM SET – 1-2
KINETIC THEORY OF GASES

1. What is the ratio of the probability that a gas molecules have two times the mean speed to the probability that they have the mean speed?
2. For $\text{CH}_4(\text{g})$ at 300 K and 1 bar, calculate the probability that a molecule picked at random has its speed in the range 400.000 to 400.001 m/s. This interval is small enough to be considered infinitesimal.
3. For CO_2 at 500 K and for N_2 at 300 K calculate
(a) $\langle v^2 \rangle^{1/2}$ (b) $\langle v \rangle$ (c) v_{mp}
4. Find the molecular weight of hydrocarbon gas that effuses 0.872 times as fast as O_2 through a small hole the temperatures and pressures being equal.
5. Use $F(v)dv$ function for v to find $\langle v^3 \rangle$ for ideal gas molecule. Does $\langle v^3 \rangle$ equal to $\langle v^2 \rangle \langle v \rangle$.
6. Calculate the total molecular translational kinetic energy at 25 °C and 1 atm for 2 moles of N_2 .
7. The average translational kinetic energy for a molecule (ϵ) is given by
$$\epsilon = \frac{1}{2} m \langle v^2 \rangle$$
where m is the mass of the molecule and $\langle v^2 \rangle$ is the average of the square of the velocity. Given $\langle v^2 \rangle = \frac{3kT}{m}$, where k is Boltzmann's constant, calculate the ratio of the kinetic energies at 200 °C and 100 °C.
8. For 1.00 mol of O_2 at 300 K and 1.00 atm, calculate (a) the number of molecules whose speed lies in the range 500.00 to 500.001 m/s (b) the number of molecules with v_z in the range 150.00 to 150.002 m/s
9. For molecular oxygen at 25 °C, a) Define collision frequency, b) Define collision density.
c) calculate the collision frequency Z_1 and the collision density Z_{11} at a pressure of 1 bar. ($d_{\text{O}_2} = 3.61 \times 10^{-10}$ m)
10. What are the mean free paths in meters for O_2 at (a) 1 bar pressure and (b) 0.1 Pa pressure?
11. For an equimolar mixture of H_2 and I_2 at 500 K and 1 atm, calculate the number of collisions per second per cm^3 between H_2 - H_2 and H_2 - I_2 molecules. ($d_{\text{H}_2} = 2.18 \times 10^{-8}$ cm) ($d_{\text{I}_2} = 3.76 \times 10^{-8}$ cm)
12. Find \bar{v} for (a) H_2 at 0 °C and 1 atm, (b) N_2 at 25 °C and 1 atm.
13. For a gas with collision diameter of 3×10^{-8} cm, calculate the mean free path at 0 °C and 1 atm.
14. Calculate the thermal conductivity of Argon at 300 K and 15 Mbar. Gas is confined in a cubic vessel of side 15 cm, one wall being 305 K and one opposite at 295 K. What is the rate of flow of energy as heat from one wall to the other?
15. For 1.00 mol of O_2 at 300 K and 1.00 atm, calculate (a) the number of molecules whose speed lies in the range 500.00 to 500.001 m/s (b) the number of molecules with v_z in the range 150.00 to 150.002 m/s (c) the number of molecules that simultaneously have v_z in the range 150.00 to 150.001 m/s and have v_x in the range 150.00 to 150.001 m/s.